

A STUDY AND MATHEMATICAL MODELING OF SYNTHETIC APERTURE RADAR (SAR) MISSILE

JOGINDER SINGH, RAHUL KAKKAR, SUMEET GOYAL and GURINDERJIT KAUR

CGC College of Engineering Landran, India E-mail: cgccoe.appsc.jsa@gmail.com cgccoe.appsc.sug@gmail.com

Abstract

In the modern era, to increase the accuracy for any missile the guidance system is mostly automatic. The target should be identified accurately so that the missile can be guided towards it to provide better defense. Synthetic Aperture Radar imaging are having numerous advantages like remote imaging, improved guidance accuracy and better functioning in all day and all weathers. A study on formation for SAR image, SAR missile and its mathematical modeling is discussed in this paper. Analysis of SAR sub-aperture algorithm is done in this study. The technique can be used provide data for targeting before launch or during flight.

1. Introduction

SAR means Synthetic Aperture Radar. SAR is the advanced technique of radar imaging. Two dimensional and three dimensional images are created using this form of radar. High resolution is required for the images at a broader level in the mapping of the earth resources, in military systems and in the monitoring of environment [1-3]. The imaging required in this type of imaging acquires in unpleasant weather or at the night and such capability is provided by Synthetic Aperture Radar (SAR). [4] The radar signals have the propagation of very long range and advantage of this characteristic of radar signals is taken by Synthetic Aperture Radar (SAR). The imagery of high

²⁰¹⁰ Mathematics Subject Classification: 00A71.

Keywords: SAR; Imaging; Azimuth Process; Radar; Microwaves; target; Digital signal processing.

Received September 23, 2019; Accepted December 16, 2019

J. SINGH, R. KAKKAR, S. GOYAL and G. KAUR

334

resolution is provided by modern digital electronics which has the capability of processing complex information [5-6]. The capabilities of optical imaging and photographic imaging are complemented by SAR because the atmospheric conditions cannot limit it [7-9].



Figure 1. Transmission of radar pulse.

Transmission of microwave pulses takes places towards the surface of the earth in SAR imaging. The spacecraft measures the microwave energy which is scattered back [10-12]. Now the simple radar principle is used by SAR system in which the image is formed by capturing the time delay caused by the microwave energy signals which were scattered back [13].



Figure 2. Backscatter of radar pulse to antenna.

The radar signal which is reflected back is driven by the backscatter radar which contains information regarding the surface of the earth. There are many factors which drive this reflection [14-16]. These factors include radar parameters and surface parameters. Radar parameters are polarization, frequency, and wavelength and incidence angle. Surface parameters are dielectric constant, roughness of the surface and the orientation and surface of the objects [17].

2. Algorithm for SAR Image Formation

The algorithm used for the formation of SAR image usually consists of two algorithms. These are RD algorithm and azimuthal preprocess. The work flow is as given in the figure below.



Figure 3. System Flow.

Firstly, the data which is sampled from A/D converter or the input data is sent for the caching of the data in FGPA and further it is transferred to azimuthal preprocess. In this process the rate of the data transfer is lowered so that the data is suitable for the DSP processing. Then the range processing of the data is done in the next module followed by the transport storage. The azimuth processing is carried out when the data from the cache is read. The computing modulus provides the final output. This algorithm has many advantages such as easy implementation and less calculations. The disadvantage of this algorithm is that the input signal spectrum is stationary because the signal is passed through band pass filter with constant coefficient [18-20].

The basic principle on which the SAR system is explained as follows. High azimuth resolution is obtained by signal processing when the target and the radar have relative motion between them and hence a long aperture is formed. When the filter velocity matched with azimuth equals the platform speed then the best focus is obtained when the target is stationary [21-22]. However when the target is moving, then the relative speed between the target and the platform is considered to obtain the best azimuth focus.

3. Analysis of SAR Missile Sub-Aperture Algorithm

The Doppler bandwidth is very large in azimuth due to the high speed of the missile and due to this there is very high scope of spectrum alias and so the PRF (Pulse Repetition Frequency) must be very high [23]. In order to lower the data transfer rate so that it is suitable for real time processing, an algorithm is required based on sub-aperture and is in time domain [24]. It is better that the sub aperture time is shorter for the amount of data to decrease. The azimuth resolution is given as:

$$\delta_a = \frac{V_a}{B_a} = \frac{V_a}{f_{dr} \cdot \Delta T_S} \,. \tag{1}$$

Here, delta represents the azimuth resolution, V_a represents the velocity of missile, B_a represents the Doppler bandwidth and T_S is the time of sub-aperture. The resolution is higher when the sub-aperture time is higher. There are basic steps which are to be followed for this algorithm. Firstly, the pulse compression is carried out with echo signal at range direction. The expression for range reference function is given as:

$$H(f) = \exp\left[j\pi\left(\frac{f^2}{K_r}\right)\right].$$
(2)

Here, f denotes the frequency and K_r is LFM signal slope.

The expression for the output signal is given as:

$$S_r(t, \tau) = \sin c \left\{ \pi B \left[\tau - \frac{2r(t)}{c} \right] \right\} \cdot \exp \left[-j \frac{4\pi r(t)}{\lambda} \right].$$
(3)

Here, Γ is the range time, *t* is the azimuth time, r(t) is the transient distance and *b* is the LFM signal bandwidth. The expression for r(t) is given as:

$$r(t) = r_0 - \frac{\lambda f_{dc}}{2} t - \frac{\lambda f_{dr}}{4} t^2.$$
 (4)

The distance between point target and radar is given by r_0 and f_{dc} represents the Doppler frequency. The expression of f_{dc} is given by:

$$f_{dc} = \frac{2v \cdot \sin \theta_0}{\lambda} \tag{5}$$

 θ_0 represents the deviated angle from the central line of the beam along azimuth. Inserting the expression of r(t) in equation (3) we get:

$$S_{r}(t, \tau) = \sin c \left[\pi B \left(\tau - \frac{2r_{0}}{c} + \frac{f_{dc}}{f_{c}} t + \frac{f_{dr}}{2f_{c}} t^{2} \right) \right]$$
$$\cdot \exp \left[-j \frac{4\pi r_{0}}{\lambda} \right] \cdot \exp \left(j 2\pi f_{dc} t + j \pi f_{dr} t^{2} \right), \tag{6}$$

where f_c is frequency of the carrier wave.

The range walk migration is given by the first order function of t in sin c. The sin c function is given as:

$$\sin c \bigg[\pi B \bigg(\tau - \frac{2r_0}{c} \bigg) \bigg].$$

The Fourier transform $S_{r1}(f)$ is given as:

$$F\left\{\sin c \left[\pi B\left(\tau - \frac{2r_0}{C}\right)\right]\right\} = S_{r1}(f).$$
⁽⁷⁾

Then,

$$F\left\{\sin c\left[\pi B\left(\tau - \frac{2r_0}{C} + \frac{f_{dc}}{f_c}t + \frac{f_{dr}}{2f_c}t^2\right)\right]\right\} = S_{r1}(f) \cdot \exp\left(j2\pi \frac{f_{dc}}{f_c}ft\right) \cdot \exp\left(j\pi \frac{f_{dr}}{f_c}ft^2\right).$$
(8)

A compensation factor ϕ is multiplied in frequency domain to carry out the RCMC (Range Cell Migration Correction) after the multiplication with reference function.

$$\phi_1 = \exp\left(-j2\pi \frac{f_{dc}}{f_c} ft\right) \tag{9}$$

 f_{dc} represents the centroid of Doppler. A rough estimation of f_{dc} is made to satisfy the condition of real time processing. This is done by collecting the data from INS (Indian navigational Services) and then clutter clock is used for making the precise estimation [25]. The curvature range is represented in the sin *c* function by the term t^2 . RCMC neglects the range curvature influence using the compensation factor given as:

$$\phi_2 = \exp\left(-j2\pi f_{dc}t - j\pi f_{dr}t^2\right). \tag{10}$$

The flowchart of the sub-aperture algorithm in the time domain is shown in figure 3



Figure 3. Flowchart of the algorithm.

4. Conclusion

SAR is imaging technique using RADAR that produces high resolution images of a scene by producing coherent phase history of reflected signal over multiple pulses being transmitted. With the increase in the techniques of homing guidance, SAR provides better accuracy even in bad weather conditions. Missile borne SAR can improve inertial guidance system for long range missiles. In this paper, forming of SAR image, sub aperture algorithm has been discussed with mathematical modeling.

References

- [1] Chan, Yee Kit and Voon Chet Koo, An introduction to synthetic aperture radar (SAR), Progress In Electromagnetics Research 2 (2008), 27-60.
- [2] Philip J. Hajduk, SAR by NMR: putting the pieces together, Molecular interventions 6(5) (2006), 266-272.
- [3] Süb, Martin, Bernhard Grafmüller and Rolf Zahn, A novel high resolution, wide swath SAR system, In IGARSS 2001, Scanning the Present and Resolving the Future. Proceedings, IEEE 2001 International Geoscience and Remote Sensing Symposium (Cat. No. 01CH37217), vol. 3, pp. 1013-1015. IEEE, 2001.
- [4] Peltason, Lisa and Jürgen Bajorath, SAR index: quantifying the nature of structureactivity relationships, Journal of medicinal chemistry 50(23) (2007), 5571-5578.
- [5] Hein and Achim, Processing of SAR data, Springer-Verlag, 2003.

Advances and Applications in Mathematical Sciences, Volume 19, Issue 5, March 2020

338

- [6] Cellier, François, Hélène Oriot and Jean-Marie Nicolas, Introduction of the mean shift algorithm in SAR imagery: Application to shadow extraction for building reconstruction, In Proceedings of the Earsel 3D Remote Sensing Workshop, Porto, Portugal, (2005), 6-11.
- [7] C. Wu, B. Barkan, B. Huneycutt, C. Leang and S. Pang, An introduction to the interim digital SAR processor and the characteristics of the associated Seasat SAR imagery, (1981).
- [8] Sharma, Manvinder and Harjinder Singh, SIW based Leaky wave antenna with Semi C-shaped slots and its Modeling, Design and parametric considerations for different materials of Dielectric, In 2018 Fifth International Conference on Parallel, Distributed and Grid Computing (PDGC), pp. 252-258. IEEE, 2018.
- [9] Ronald L. Seaman and Robert M. Lebovitz, Thresholds of cat cochlear nucleus neurons to microwave pulses, Bioelectromagnetics: Journal of the Bioelectromagnetics Society, The Society for Physical Regulation in Biology and Medicine, The European Bioelectromagnetics Association 10(2) (1989), 147-160.
- [10] Kaur, Sanam Preet and Manvinder Sharma, Radially optimized zone-divided energyaware wireless sensor networks (WSN) protocol using BA (bat algorithm), IETE Journal of Research 61(2) (2015), 170-179.
- [11] Wang, Xiong, Daniel R. Bauer, Jeff L. Vollin, David G. Manzi, Russell S. Witte and Hao Xin, Impact of microwave pulses on thermoacoustic imaging applications, IEEE Antennas and Wireless Propagation Letters 11 (2012), 1634-1637.
- [12] Joseph T. Case, Mohammad Tayeb Ghasr and Reza Zoughi, Optimum two-dimensional uniform spatial sampling for microwave SAR-based NDE imaging systems, IEEE Transactions on Instrumentation and Measurement 60(12) (2011), 3806-3815.
- [13] Joseph T. Case, Mohammad Tayeb Ghasr, and Reza Zoughi, Optimum 2-D nonuniform spatial sampling for microwave SAR-based NDE imaging systems, IEEE Transactions on Instrumentation and Measurement 61(11) (2012), 3072-3083.
- [14] Sharma, Manvinder, Sohni Singh, Dishant Khosla, Sumeet Goyal and Anuj Gupta, Waveguide Diplexer: Design and Analysis for 5G Communication, In 2018 Fifth International Conference on Parallel, Distributed and Grid Computing (PDGC), pp. 586-590. IEEE, 2018.
- [15] Werness, A. S. Susan, Walter G. Carrara, L. S. Joyce and David B. Franczak, Moving target imaging algorithm for SAR data, IEEE Transactions on Aerospace and Electronic Systems 26(1) (1990), 57-67.
- [16] Ding, Yu and D. C. Jr. Munson, A fast back-projection algorithm for bistatic SAR imaging, In Proceedings, International Conference on Image Processing, vol. 2, pp. II-II. IEEE, 2002.
- [17] De Graaf and R. Stuart, SAR imaging via modern 2-D spectral estimation methods, IEEE Transactions on Image Processing 7(5) (1998), 729-761.
- [18] H. S. Shin and J. T. Lim, Omega-k algorithm for airborne forward-looking bistatic spotlight SAR imaging. IEEE Geoscience and Remote Sensing Letters 6(2) (2009), 312-316.

340 J. SINGH, R. KAKKAR, S. GOYAL and G. KAUR

- [19] Wei, Shun-Jun, Xiao-Ling Zhang, Jun Shi and Gao Xiang, Sparse reconstruction for SAR imaging based on compressed sensing, Progress In Electromagnetics Research 109 (2010), 63-81.
- [20] Manvinder Sharma and Harjinder Singh, Substrate Integrated Waveguide Based Leaky Wave Antenna for High Frequency Applications and IoT, International Journal of Sensors, Wireless Communications and Control (2019) 9: 1. https://doi.org/10.2174/2210327909666190401210659
- [21] Bamler and Richard, A comparison of range-Doppler and wavenumber domain SAR focusing algorithms, IEEE Transactions on Geoscience and Remote Sensing 30(4) (1992), 706-713.
- [22] Gao, Shesheng, Yongmin Zhong, Xueyuan Zhang and Bijan Shirinzadeh, Multi-sensor optimal data fusion for INS/GPS/SAR integrated navigation system, Aerospace Science and Technology 13(4-5) (2009), 232-237.
- [23] Kaur, Navpreet and Manvinder Sharma, Brain tumor detection using self-adaptive Kmeans clustering, In 2017 International Conference on Energy, Communication, Data Analytics and Soft Computing (ICECDS), pp. 1861-1865. IEEE, 2017.
- [24] Liu, Jian-Ye, Zhi Xiong and Fang Duan, Processing the measurement delay INS/SAR integrated navigation in-coordinate interval filtering algorithm study, Yuhang Xuebao/Journal of Astronautics(China) 25(6) (2004), 626-631.